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Design for high-power, single-lobe, grating-surface-emitting quantum cascade lasers enabled by plasmon-enhanced absorption of antisymmetric modes

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Resonant coupling of the transverse-magnetic polarized (guided) optical mode of a quantum-cascade laser (QCL) to the antisymmetric surface-plasmon modes of 2nd-order distributed-feedback (DFB) metal/semiconductor gratings results in strong antisymmetric-mode absorption. In turn, lasing in the symmetric mode, that is, surface emission in a single-lobe far-field beam pattern, is strongly favored over controllable ranges in grating duty cycle and tooth height. By using core-region characteristics of a published 4.6 μm -emitting QCL, grating-coupled surface-emitting (SE) QCLs are analyzed and optimized for highly efficient single-lobe operation. For infinite-length devices, it is found that when the antisymmetric mode is resonantly absorbed, the symmetric mode has negligible absorption loss ($\sim 0.1 \text{ cm}^{-1}$) while still being efficiently outcoupled, through the substrate, by the DFB grating. For finite-length devices, 2nd-order distributed Bragg reflector (DBR) gratings are used on both sides of the DFB grating to prevent uncontrolled reflections from cleaved facets. Equations for the threshold-current density and the differential quantum efficiency of SE DFB/DBR QCLs are derived. For 7 mm-long, 8.0 μm -wide, 4.6 μm -emitting devices, with an Ag/InP grating of $\sim 39\%$ duty cycle, and $\sim 0.22 \mu\text{m}$ tooth height, threshold currents as low as 0.45 A are projected. Based on experimentally obtained internal efficiency values from high-performance QCLs, slope efficiencies as high as 3.4 W/A are projected; thus, offering a solution for watt-range, single-lobe CW operation from SE, mid-infrared QCLs. © 2014 AIP Publishing LLC. [<http://dx.doi.org/10.1063/1.4869561>]

Grating-coupled surface-emitting lasers (GCSEL) are attractive sources due to easy packaging, lack of emitting-facet heating and subsequent degradation, ability to reach 1 W diffraction-limited continuous-wave (CW) power,¹ and the potential for obtaining multi-watt CW diffraction-limited power when combined with single-lateral-mode, high-index-contrast photonic-crystal structures.²

Research on GCSELs started in the early 1970s and was focused on near-infrared (IR)-emitting devices.^{3–6} It was found for TE-polarized lasers that, in accordance with theory,⁷ the longitudinal mode favored to lase is the antisymmetric one (i.e., a mode whose far-field pattern consists of two lobes) due to its inherent low radiation loss and subsequent low threshold gain. Several approaches have been proposed and demonstrated for realizing operation in a single-lobe beam⁸ with the most successful ones being those involving no penalty in efficiency: central grating π phase shift^{9–11} or chirped grating corresponding to a π phase shift.¹

With the advent of quantum cascade lasers (QCLs) in the mid 1990s, GCSEL analysis turned to devices generating transverse-magnetic (TM)-polarized light.¹² SE distributed-feedback (DFB) grating, mid-IR-emitting QCLs include: two-dimensional (2-D) photonic-crystal structures,¹³ air-metal/semiconductor gratings,¹⁴ metal/semiconductor gratings for emission only through the substrate,^{15,16} metal/semiconductor biperiodic gratings,¹⁷ and all-semiconductor gratings.^{18,19} By

and large, the antisymmetric mode was found to be favored to lase, just like for TE-polarized GCSELs, with two exceptions: (a) excitation of a 2nd-order DFB region from a 1st-order DFB laser¹⁶ which gave a single, diffraction-limited beam only for short ($\leq 200 \mu\text{m}$) apertures and (b) an edge- and surface-emitting device¹⁹ that provided 100 mW CW surface-emitted power in a near-diffraction-limited beam, with significant power being edge emitted, and occasional two-lobed beams due to uncontrolled facet reflections. 500 mW CW surface-emitted power was reported from ring-cavity devices,¹⁸ but operating multimode. More recently,²⁰ ring-cavity GCSE QCLs have provided a symmetric-like, multilobe beam pattern, as a result of employing two π phase shifts and a linear-polarization scheme. THz SE-DFB QCLs have been found to operate in the antisymmetric mode as well with the solution for single-lobe operation being either a central π phase shift^{21,22} or symmetric-mode selection via dual-slit unit-cell gratings²³ or gratings chirped from their centers to their edges.²⁴ Furthermore, by using resonant leaky-wave coupling,^{25,26} 2-D GCSE THz QCLs emitting in diffraction-limited beams have been demonstrated.^{27,28}

Here, we present a GCSE QCL mid-IR-emitting structure with inherent suppression of the antisymmetric modes that allows symmetric-mode lasing at low ($< 0.5 \text{ A}$) threshold currents and high ($> 3 \text{ W/A}$) slope efficiencies. The device relies on the antisymmetric modes being strongly absorbed due to resonant coupling of the (guided) optical mode to the antisymmetric surface plasmon mode of a metal/semiconductor grating. In addition, the DFB grating is bounded by 2nd-order

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distributed Bragg reflector (DBR) gratings;^{1,8–10} thus, preventing uncontrolled reflections from cleaved facets, which can affect the DFB operation,¹⁹ as well as catastrophic facet degradation at high powers due to the thermally induced shear stress.²⁹ By considering a $4.6\text{ }\mu\text{m}$ -emitting QCL structure which was previously reported to edge-emit watt-range CW power,³⁰ we find that 7.03 mm -long DFB/DBR GCSE devices can have threshold currents as low as 0.45 A and slope efficiencies as high as 3.4 W/A ; thus, making it possible to obtain watts of CW diffraction-limited, single-lobe power from mid-IR surface-emitting QCLs. First, we analyze devices of infinite-length metal/semiconductor 2nd-order DFB gratings, in order to elucidate the mechanism via which the antisymmetric mode is suppressed. Then, we present the design and analysis of 2nd-order DFB/DBR devices of finite-length gratings, and provide examples of high-performance devices.

The antisymmetric surface plasmon mode at the interface(s) of a 2nd-order metal/semiconductor has its H-field intensity nulls occur in the middle of the grating troughs and peaks [see example in Fig. 1(b)]. For an infinite-length grating with Ag for metal, InP for semiconductor and designed to be the 2nd-order DFB grating for a published³⁰ $4.6\text{ }\mu\text{m}$ -emitting QCL structure, we plot in Fig. 1(a) the wavevector of the plasmon as a function of grating duty cycle, defined as the percentage of metal in a grating period, and grating tooth height. A thin white line indicates the plasmon-wavevector curve corresponding to $4.6\text{ }\mu\text{m}$ wavelength, λ ; that is, where the DFB-QCL structure's optical-mode propagation constant matches the plasmon-mode propagation constant, and thus resonant coupling occurs between the two modes. We show in Fig. 1(b)

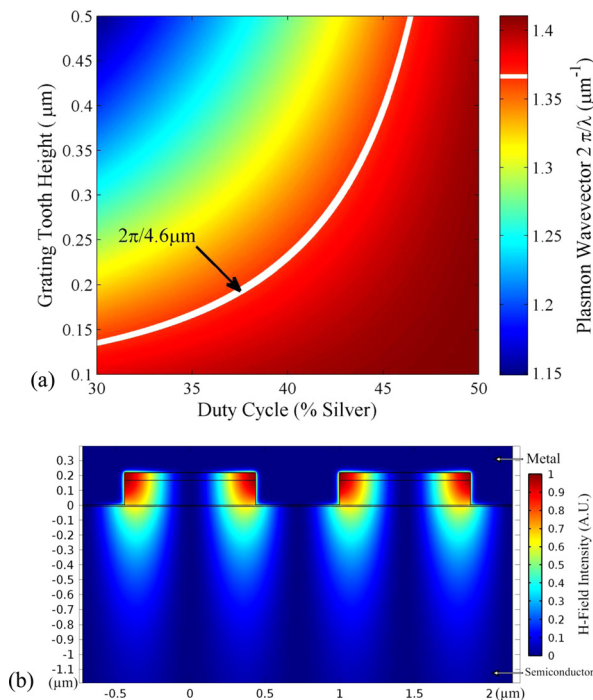


FIG. 1. Infinite-length grating: (a) Plasmon wavevector as function of grating duty cycle and tooth height for Ag/InP grating designed to be 2nd-order DFB grating for a published $4.6\text{ }\mu\text{m}$ -emitting QCL.³⁰ The white line corresponds to resonant coupling between the (guided) optical mode and the antisymmetric plasmon mode; (b) H-field intensity pattern at a resonance point: 39% duty cycle and $0.217\text{ }\mu\text{m}$ grating tooth height, at $\lambda = 4.6\text{ }\mu\text{m}$.

the plasmon H-field intensity for a grating of 39% duty cycle and $0.217\text{ }\mu\text{m}$ tooth height ($\lambda = 4.6\text{ }\mu\text{m}$).

Next, we consider the DFB-QCL structure for which the (transverse) optical mode couples to the grating surface-plasmon modes. Coupling to the antisymmetric and symmetric plasmon modes results in antisymmetric (A) and symmetric (S) longitudinal modes of the structure. We choose a 40-period, $4.6\text{ }\mu\text{m}$ -emitting QCL structure³⁰ of 75% transverse optical-confinement factor Γ . The grating period Λ is fixed to be that ratio of the vacuum wavelength ($4.6\text{ }\mu\text{m}$) to the effective refractive index of the transverse mode, such that the 2nd-order Bragg-diffraction condition is met. For this 2nd-order DFB-QCL structure, we show in Fig. 2 the dispersion curves, at 39% grating duty cycle, for the A and S modes as a function of tooth height, h . As seen from the inserted pictures, in the case of the A mode for $h < 0.217\text{ }\mu\text{m}$ the guided mode couples in-phase with the antisymmetric plasmon mode, while for $h > 0.217\text{ }\mu\text{m}$ the guided mode couples out-of-phase with the antisymmetric plasmon mode. The S mode couples weakly to the symmetric plasmon mode, as evidenced by negligible field at the grating interfaces. (However, the S-mode couples strongly to the grating and is effectively outcoupled over a large range in h [Fig. 3(b)].) Such modal behavior is somewhat similar to that for the modes of 1st-order metal/semiconductor DFB structures,³¹ in that the A and S modes qualitatively behave like the 1st-order DFB modes whose H-field maxima occur on the grating troughs and peaks, respectively (Fig. 3 in Ref. 31).

Fig. 3(a) shows the A-mode loss as a function of grating height and duty cycle. We superimpose the white line from Fig. 1(a) on the locus of maximum-loss points, to highlight that the latter corresponds to resonant coupling between guided and plasmon modes. The losses for the A and S modes are shown in Fig. 3(b) as the grating height varies, when the duty cycle is 39%. The A-mode loss is only absorption loss which is peaked at resonance (i.e., at $h = 0.217\text{ }\mu\text{m}$). The S mode has both surface-emission (coupling coefficient $\kappa = 0.193 - i9.231\text{ cm}^{-1}$) and absorption losses; the latter being negligible ($\sim 0.1\text{ cm}^{-1}$) due to weak optical-mode coupling to the symmetric plasmon mode. We note that significantly enhanced absorption of incident TM-polarized light, due to strong coupling to a surface-plasmon mode of a

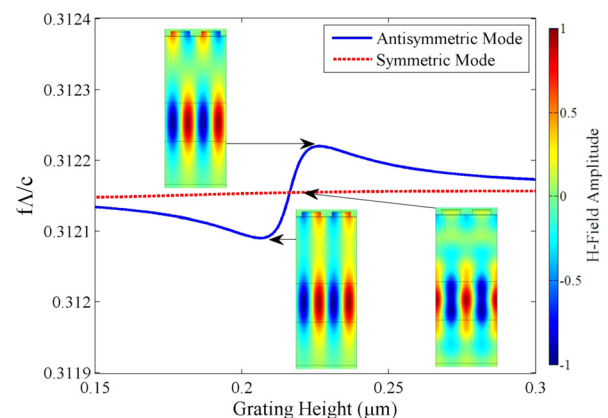


FIG. 2. Normalized frequencies for the symmetric (S) and antisymmetric (A) modes of $4.6\text{ }\mu\text{m}$ -emitting 2nd-order DFB-QCL structure, at 39% grating duty cycle, as a function of grating tooth height, h . Insets: H-field amplitude patterns. The A-mode is shown below and above resonance at $h = 0.217\text{ }\mu\text{m}$.

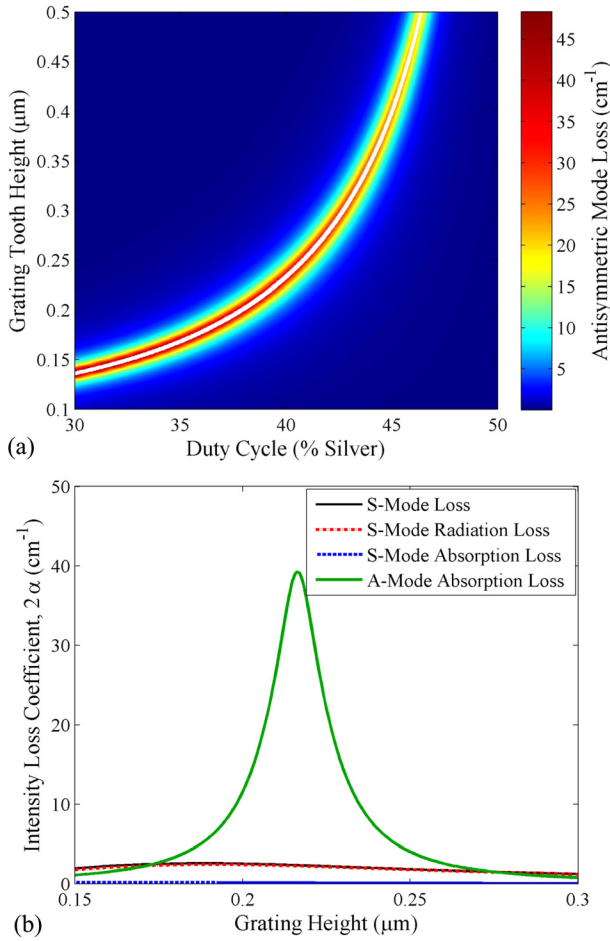


FIG. 3. (a) The antisymmetric (A)-mode loss as a function of grating duty cycle and tooth height. The white line atop the locus of maximum-loss points is the same white line as in Fig. 1(a), confirming that the A-mode maximum loss occurs at grating parameters corresponding to resonant coupling between guided and plasmon modes. (b) Intensity loss coefficient⁸ for the symmetric and antisymmetric modes as a function of grating height when the grating duty cycle is 39%. The S-mode absorption loss is negligible.

2nd-order DFB metal grating, has previously been obtained³² for proposed high-performance mid-IR photodetectors.

Next, we study finite-length, buried-heterostructure devices with DBR gratings at the ends of the DFB grating (Fig. 4), just as for high-power, near-IR GCSELS.^{1,8-10} A longitudinal cross-section is shown in the inset. The 40-period InGaAs/InAlAs core region of a high-CW-power, 4.6 μm-emitting QCL³⁰ is considered. Atop an InP cladding layer a metal/semiconductor grating is placed. To control the tooth height, a 10 nm-thick InGaAs etch-stop layer [Fig. 1(b)] is introduced between the InP cladding layer and the grating. At the top of the semiconductor portions of the grating, a 50 nm-thick n⁺-InP layer is added [Fig. 1(b)] to ensure good electrical contact, and 2 nm-thick Ti layers are inserted between metal and semiconductor for good adhesion.

For finite-length devices, the coupled-mode theory for 2nd-order metal/semiconductor gratings is employed⁷ together with the matrix method for DFB/DBR structures⁸ adjusted for TM-polarized light. More specifically, COMSOL is used to calculate the eigenfrequencies of the symmetric and antisymmetric modes for an infinite-length DFB structure.⁷ The real and imaginary parts of these are converted into detuning and loss parameters, both in units of

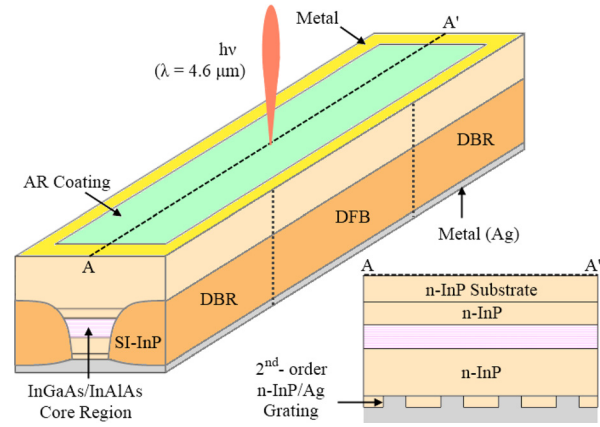


FIG. 4. Schematic representation of surface-emitting, buried-heterostructure DFB/DBR QCL for operation at 4.6 μm wavelength.

cm⁻¹, and then inserted into the equations for calculating the coupling coefficient and correction factor.⁷ Then, we use the transfer-matrix method to solve for the grating-related (intensity) loss coefficient,⁸ 2α, which is part of the *local* threshold gain (i.e., in the DFB region) g_{th},^{2,8} which, for interband-transition devices, is given by

$$g_{th} = 2\alpha + \frac{\alpha_i}{\Gamma_{lg}}, \quad (1)$$

where α_i is the internal cavity loss and Γ_{lg} is the percentage of field intensity residing in the DFB region. However, for QCLs one has to take into account the backfilling-current density³³ and the leakage-current density³³ which, multiplied by Γ_g, are routinely subsumed with α_i as being parts of a “waveguide” loss coefficient α_w in the threshold-current density formula for Fabry-Perot-cavity devices: J_{th} = (α_m + α_w)/Γ_g, where α_m is the mirror loss and g is the differential gain. Since backfilling and carrier leakage occur only in the DFB region, the g_{th} equation for SE DFB/DBR QCLs is

$$g_{th,q} = 2\alpha + \alpha_w + \left(\frac{1}{\Gamma_{lg}} - 1\right)\alpha_i. \quad (2)$$

For α_w we take the experimental value obtained³⁰ by Lyakh *et al.*: 3.3 cm⁻¹, and for α_i we take a value of 0.5 cm⁻¹, typical of state-of-the-art, high-power 4.5–5.0 μm-emitting QCLs.^{34,35} The modal threshold gain² G_{th,q} = Γ_{lg}g_{th,q}. Then, the threshold-current density is

$$J_{th} = \frac{G_{th,q}}{\Gamma_{lg}\Gamma_g} = \frac{g_{th,q}}{\Gamma_g}. \quad (3)$$

The finite-length structure chosen for analysis is one that maximizes the outcoupling loss for the S mode, while maintaining a low value (i.e., 2) for the S-mode guided-field-intensity peak-to-valley ratio in the DFB region⁸ R₀; chosen to prevent multimoding at high-drive levels due to longitudinal gain spatial hole burning. Then, for a 7.03 mm-long device of 3.07 mm-long DFB region and 1.98 mm-long DBR regions, we find for the S mode that 2α = 5.98 cm⁻¹ and Γ_{lg} = 0.81. In turn, g_{th,q} has a value of 9.4 cm⁻¹ and the G_{th} value is 7.6 cm⁻¹. Fig. 5(a) shows the g_{th,q} values for A and S modes, as a function of detuning from the reference 4.6 μm wavelength, for a grating of 39% duty cycle and 0.217 μm height.

An S mode is clearly favored to lase over two adjacent A modes, which have $g_{\text{th},q}$ values 23.1 cm^{-1} and 23.9 cm^{-1} higher than the S mode. These large intermodal-discrimination values are dominated by the strong absorption of the A modes. For the S mode, by using Eq. (3) and the g value experimentally obtained by Lyakh *et al.*,³⁰ we obtain a J_{th} value of 1.84 kA/cm^2 . Then, for a 3.07 mm -long DFB region and a $8.0 \mu\text{m}$ -wide buried-ridge guide,³⁶ as needed for operation primarily in the fundamental lateral mode,³⁷ the threshold current is 0.45 A , a value comparable to those of state-of-the-art, high-power edge-emitting QCLs operating in the $4.5\text{--}5.0 \mu\text{m}$ range.^{34,35}

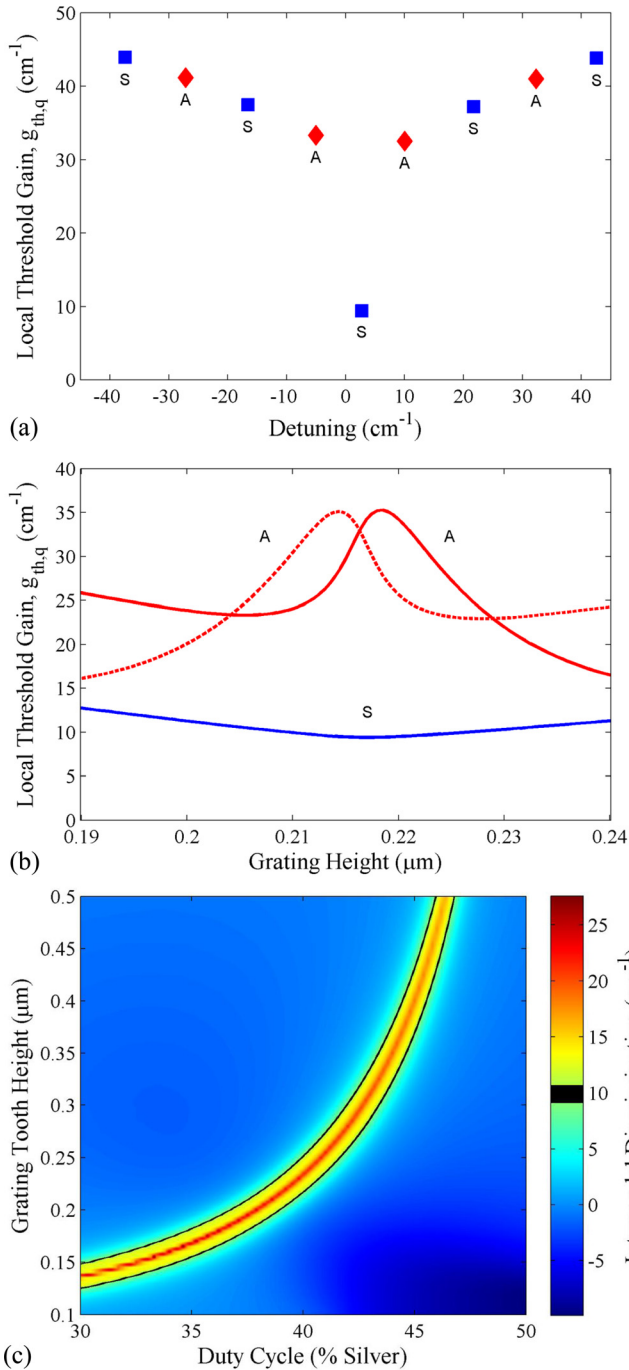


FIG. 5. (a) Local threshold gain $g_{\text{th},q}$ for S and A modes, at 39% duty cycle and $0.217 \mu\text{m}$ grating height, as a function of detuning from the $4.6 \mu\text{m}$ reference wavelength. (b) $g_{\text{th},q}$ for S and A modes vs. grating height, at 39% duty cycle. (c) Intermodal discrimination vs. grating height and duty cycle.

Fig. 5(b) shows the $g_{\text{th},q}$ values for the S and the two adjacent A modes as a function of grating height, at 39% duty cycle. The A modes reach $g_{\text{th},q}$ maxima at values corresponding to resonant coupling of the guided mode to the anti-symmetric plasmon mode, at their respective oscillation wavelength. The intermodal discrimination is $\geq 10 \text{ cm}^{-1}$ over a $0.030 \mu\text{m}$ -wide variation in tooth height, which is quite achievable by using a stop-etch layer. Fig. 5(c) shows the intermodal discrimination as a function of duty cycle and tooth height. Thin black lines indicate where the intermodal discrimination is 10 cm^{-1} ; thus, defining a curved-stripe-shaped domain over which the intermodal discrimination is $\geq 10 \text{ cm}^{-1}$. For a fixed duty cycle, intermodal discrimination is $\geq 10 \text{ cm}^{-1}$ over a $0.030 \mu\text{m}$ -wide variation in tooth height (e.g., over the $0.202\text{--}0.232 \mu\text{m}$ range in tooth height at 39% duty cycle). This can easily be achieved by using the InGaAs stop-etch layer. For a fixed tooth height, intermodal discrimination is $\geq 10 \text{ cm}^{-1}$ over a 2%-wide variation in duty cycle (e.g., over the 38%–40% range in duty cycle at $0.217 \mu\text{m}$ tooth height). For a grating of $1.44 \mu\text{m}$ period, this corresponds to controlling the tooth width within $0.03 \mu\text{m}$, which can be achieved with e-beam lithography.

A study over the ranges: 37%–41% in duty cycle and $0.202\text{--}0.232 \mu\text{m}$ in grating height, within the $\geq 10 \text{ cm}^{-1}$ domain, reveals that the grating outcoupling efficiency decreases by at most 15% (i.e., from 40% to 34%). 40% outcoupling efficiency is obtained for 38%, 39% and 40% duty cycle at $0.202 \mu\text{m}$, $0.217 \mu\text{m}$ and $0.232 \mu\text{m}$ grating height, respectively. Thus, the chance of getting outcoupling efficiencies close to 40% is high. Finally, if the grating height is controlled, via the etch-stop layer, to be within the $0.03 \mu\text{m}$ range, the range of acceptable duty-cycle values is 4%: from 37% to 41%; thus, the actual tolerance in grating-tooth width is $0.06 \mu\text{m}$, which can be controlled via e-beam lithography.

Figs. 6(a) and 6(b) show the radiated near-field intensity^{8,9} and the envelope of the guided-field intensity profiles for S and A modes, when the grating duty cycle and tooth height are 39% and $0.217 \mu\text{m}$. The R_0 value is only 2, as required to ensure single-longitudinal-mode operation to high drive levels.^{1,8} For the A modes the guided-field intensity in

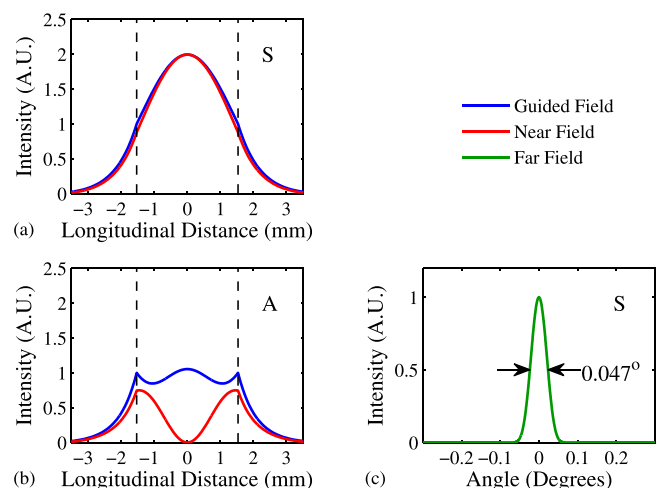


FIG. 6. Near-field intensity and envelope of guided-field intensity profiles for (a) S and (b) A modes, at 39% duty cycle and $0.217 \mu\text{m}$ grating height. (c) Far-field beam pattern for the S mode.

the DFB region is fairly uniform, yet peaks in the center of the DFB region. Considering this, the fact that the intermodal discrimination is $>20\text{ cm}^{-1}$ and that $R_0 = 2$, it is quite reasonable to assume that longitudinal spatial hole burning is unlikely to cause multimoding at high drives above threshold. Fig. 6(c) is the S-mode far-field beam pattern: a single lobe.

As for the differential quantum efficiency, the equation for GCSELS^{2,8} modified for QCLs is

$$\eta_d = \eta_i \frac{\alpha_{\text{surf}}}{G_{\text{th}}} N_p = \eta_p \eta_{\text{tr}} \frac{\alpha_{\text{surf}}}{2\alpha\Gamma_{\text{lg}} + \alpha_i} N_p, \quad (4)$$

where α_{surf} is the surface radiation loss;² η_i is the internal differential efficiency per period,³⁸ the product of η_p , the differential pumping efficiency, and η_{tr} , the transition differential efficiency; and N_p is the period number. The $\alpha_{\text{surf}}/G_{\text{th}}$ term, known as outcoupling efficiency, is 40% in this case. While for devices with suppressed carrier leakage (i.e., η_p close to unity) the η_i value is theoretically ~ 0.85 , the best reported^{35,39} experimental values are in the 0.70–0.79 range. Then, taking $N_p = 40$, $\lambda = 4.6\ \mu\text{m}$, and assuming an AR-coated window and negligible substrate absorption, the estimated slope efficiencies are 3.0–3.4 W/A, values comparable to best reported pulsed, single-facet values from 4.6 μm -emitting devices. Furthermore, for devices with $R_0 = 2.5$ the outcoupling efficiency increases to 48%; then, the slope efficiencies are in the 3.6–4.1 W/A range. Since gain spatial hole burning is not well understood in QCLs, we chose to analyze the more conservative case of $R_0 = 2$, but that does not mean that devices of $R_0 = 2.5$ are not possible candidates for single-mode operation to watt-range powers.

Using the estimated threshold and slope-efficiency values (i.e., 0.45 A and 3.4 W/A), the projected peak pulsed power at $3 \times$ threshold is 3.06 W. The coherent power can be increased via resonant leaky-wave coupling of GCSE devices in the lateral direction.^{2,27,28} In fact, we have recently demonstrated⁴⁰ in-phase mode lasing of five resonant leaky-wave-coupled QCLs. Then, considering that typically $\sim 67\%$ of the coherent power is emitted in the array main far-field lobe, for a five-element phase-locked array of DFB/DBR QCLs coherent powers in excess of 10 W become possible.

In conclusion, a type of grating-surface-emitting laser is presented that offers efficient single-lobe lasing due to the antisymmetric modes being strongly absorbed via TM-mode resonant coupling to surface plasmon modes. By employing a published QCL-core structure, we find that DFB/DBR devices can lase in a single-lobe pattern with threshold currents as low as 0.45 A and slope efficiencies as high as 3.4 W/A. Thus, the devices hold potential for watt-range CW coherent-power emission delivered reliably, since emitting-facet heating and subsequent degradation are avoided.

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¹S. H. Macomber, J. S. Mott, B. D. Schwartz, R. S. Setzko, J. J. Power, P. A. Lee, D. P. Kwo, R. M. Dixon, and J. E. Logue, *Proc. SPIE* **3001**, 42 (1997).

²S. Li and D. Botez, *IEEE J. Quantum Electron.* **43**, 655 (2007).

³R. F. Kazarinov and R. A. Suris, *Sov. Phys. Semicond.* **6**, 1184 (1973).

⁴P. Zory, *Appl. Phys. Lett.* **22**, 125 (1973).

- ⁵G. A. Evans, J. M. Hammer, N. W. Carlson, F. R. Elia, E. A. James, and J. B. Kirk, *Appl. Phys. Lett.* **49**, 314 (1986).
- ⁶K. Mitsunaga, M. Kaneya, K. Kojima, S. Noda, K. Kyuma, K. Hamanaka, and T. Nakayama, *Appl. Phys. Lett.* **50**, 1788 (1987).
- ⁷R. J. Noll and S. H. Macomber, *IEEE J. Quantum Electron.* **26**, 456 (1990).
- ⁸S. Li, G. Witjaksono, S. Macomber, and D. Botez, *IEEE J. Sel. Top. Quantum Electron.* **9**, 1153 (2003).
- ⁹G. Witjaksono and D. Botez, *Appl. Phys. Lett.* **78**, 4088 (2001).
- ¹⁰G. Witjaksono, S. Li, J. J. Lee, D. Botez, and W. K. Chan, *Appl. Phys. Lett.* **83**, 5365 (2003).
- ¹¹E. Miyai and S. Noda, *Appl. Phys. Lett.* **86**, 111113 (2005).
- ¹²N. Finger, W. Schrenk, and E. Gornik, *IEEE J. Quantum Electron.* **36**, 780 (2000).
- ¹³R. Colombelli, K. Srinivasan, M. Troccoli, O. Painter, C. F. Gmachl, D. M. Tennant, A. M. Sergent, D. L. Sivco, A. Y. Cho, and F. Capasso, *Science* **302**, 1374 (2003).
- ¹⁴C. Pflügl, M. Austerer, W. Schrenk, S. Golka, G. Strasser, R. P. Green, L. R. Wilson, J. W. Cockburn, A. B. Krysa, and J. S. Roberts, *Appl. Phys. Lett.* **86**, 211102 (2005).
- ¹⁵A. Lyakh, P. Zory, M. D'Souza, D. Botez, and D. Bour, *Appl. Phys. Lett.* **91**, 181116 (2007).
- ¹⁶G. Maisons, M. Carras, M. Garcia, B. Simozrag, and X. Marcadet, *Appl. Phys. Lett.* **98**, 021101 (2011).
- ¹⁷G. Maisons, M. Carras, M. Garcia, O. Parillaud, B. Simozrag, X. Marcadet, and A. De Rossi, *Appl. Phys. Lett.* **94**, 151104 (2009).
- ¹⁸Y. Bai, S. Tsao, N. Bandyopadhyay, S. Slivken, Q. Y. Lu, D. Caffey, M. Pushkarsky, T. Day, and M. Razeghi, *Appl. Phys. Lett.* **99**, 261104 (2011).
- ¹⁹D.-Y. Yao, J.-C. Zhang, F.-Q. Liu, N. Zhuo, F.-L. Yan, L.-J. Wang, J.-Q. Liu, and Z.-G. Wang, *Appl. Phys. Lett.* **103**, 041121 (2013).
- ²⁰C. Schwarzer, R. Szedlak, S. I. Ahn, T. Zederbauer, H. Detz, A. Andrews, W. Schrenk, and G. Strasser, *Appl. Phys. Lett.* **103**, 081101 (2013).
- ²¹S. Kumar, B. S. Williams, Q. Qin, A. W. M. Lee, and Q. Hu, *Opt. Express* **15**, 113 (2007).
- ²²G. Sevin, D. Fowler, G. Xu, F. H. Julien, R. Colombelli, S. P. Khanna, E. H. Linfield, and A. G. Davies, *Appl. Phys. Lett.* **97**, 131101 (2010).
- ²³L. Mahler, A. Tredicucci, F. Beltram, C. Walther, J. Faist, H. E. Beere, and D. A. Ritchie, *Appl. Phys. Lett.* **96**, 191109 (2010).
- ²⁴G. Xu, R. Colombelli, S. P. Khanna, A. Belarouci, X. Letartre, L. Li, E. H. Linfield, A. G. Davies, H. E. Beere, and D. A. Ritchie, *Nat. Commun.* **3**, 952 (2012).
- ²⁵D. Botez, L. J. Mawst, and G. Peterson, *Electron. Lett.* **24**, 1328 (1988).
- ²⁶D. Botez, L. J. Mawst, G. Peterson, and T. J. Roth, *Appl. Phys. Lett.* **54**, 2183 (1989).
- ²⁷T.-Y. Kao, Q. Hu, and J. L. Reno, *Appl. Phys. Lett.* **96**, 101106 (2010).
- ²⁸Y. Halioua, G. Xu, S. Moudjji, R. Colombelli, S. P. Khanna, L. Li, A. G. Davies, E. H. Linfield, H. Beere, and D. A. Ritchie, in Proceedings of 12th International Conference on Intersubband Transitions in Quantum Wells, Bolton Landing, NY, September 2013.
- ²⁹Q. Zhang, F.-Q. Liu, W. Zhang, Q. Lu, L. Wang, L. Li, and Z. Wang, *Appl. Phys. Lett.* **96**, 141117 (2010).
- ³⁰A. Lyakh, C. Pflugl, L. Diehl, Q. J. Wang, F. Capasso, X. J. Wang, J. Y. Fan, T. Tanbuk-Ek, R. Maulini, A. Tsekoun, R. Go, and C. K. N. Patel, *Appl. Phys. Lett.* **92**, 111110 (2008).
- ³¹M. Carras and A. De Rossi, *Phys. Rev. B* **74**, 235120 (2006).
- ³²Z. Yu, G. Veronis, S. Fan, and M. L. Brongersma, *Appl. Phys. Lett.* **89**, 151116 (2006).
- ³³D. Botez, S. Kumar, J. C. Shin, L. J. Mawst, I. Vurgaftman, and J. R. Meyer, *Appl. Phys. Lett.* **97**, 071101 (2010).
- ³⁴R. Maulini, A. Lyakh, A. Tsekoun, R. Go, C. Pflügl, L. Diehl, F. Capasso, and C. K. N. Patel, *Appl. Phys. Lett.* **95**, 151112 (2009).
- ³⁵Y. Bai, N. Bandyopadhyay, S. Tsao, S. Slivken, and M. Razeghi, *Appl. Phys. Lett.* **98**, 181102 (2011).
- ³⁶A COMSOL analysis of 8 μm -wide buried-ridge devices showed negligible changes: a 0.3% change in grating period and, at resonance, for 39% duty cycle, changes in tooth height from 0.217 μm to 0.215 μm ; thus, well within the 0.03 μm tolerance in grating tooth height.
- ³⁷Y. Bai, N. Bandyopadhyay, S. Tsao, E. Selcuk, S. Slivken, and M. Razeghi, *Appl. Phys. Lett.* **97**, 251104 (2010).
- ³⁸D. Botez, J. Shin, J. Kirch, C. Chang, L. Mawst, and T. Earles, *IEEE J. Sel. Top. Quantum Electron.* **19**(4), 1200312 (2013).
- ³⁹A. Wittmann, T. Gresch, E. Gini, L. Hvozdar, N. Hoyler, M. Giovannini, and J. Faist, *IEEE J. Quantum Electron.* **44**, 36 (2008).
- ⁴⁰J. D. Kirch, C.-C. Chang, C. Boyle, L. J. Mawst, D. Lindberg, T. Earles and D. Botez, Tech. Dig. IEEE/OSA Conference on Lasers and Electro-Optics, San Jose, California, 8–13 June 2014 (to be published).